

## ON SOME GENERALIZATIONS OF ENESTRÖM-KAKEYA THEOREM

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*Abstract.* In this paper, we obtain some generalizations of a well-known result of Eneström-Kakeya concerning the bounds for the moduli of the zeros of polynomials with complex coefficients which improve some known results.

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