GENERAL TAUBERIAN CONDITIONS FOR WEIGHTED MEAN METHODS OF SUMMABILITY

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Abstract. In this paper we recover convergence of a complex sequence (u_n) out of its summability by weighted means under certain supplementary conditions that control the oscillatory behavior of (u_n). As corollaries, we obtain classical Hardy-type Tauberian conditions for various weighted mean methods.

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