AN IMPROVEMENT OF ZALCMAN'S LEMMA IN C^n

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Abstract. The aim of this article is to give a proof of improving of Zalcman's lemma in C^n.

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