ON THE GROWTH OF MEROMORPHIC SOLUTIONS OF HOMOGENEOUS AND NON–HOMOGENEOUS LINEAR DIFFERENCE EQUATIONS IN TERMS OF (p,q)–ORDER

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Abstract. In this paper we have studied the growth of meromorphic solutions of higher order homogeneous and non-homogeneous linear difference equations with entire and meromorphic coefficients. We have extended and improved some results of Zhou and Zheng (2017), Belaidi and Benkarouba (2019) by using (p,q)-order and (p,q)-type.

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