

UNICITY RELATION TO ENTIRE FUNCTIONS AND THEIR DIFFERENTIAL DIFFERENCE POLYNOMIALS

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Abstract. In this article, we investigate the problem of sharing values between entire functions $f(z)$ and $f_1(z) = b_{-1} + \sum_{i=0}^n b_i f^{(k_i)}(z + i\eta)$ share two distinct values a with counted and b with ignoring multiplicities, where b_{-1} and b_i ($i = 0, 1, \dots, n$) are small meromorphic functions of $f(z)$, $k_i \geq 0$ ($i = 0, 1, \dots, n$) are integers. In relation to previous research, we obtain results that improve and generalise the findings conducted by Yang and Qi [CMFT, 20.1 (2020): 159–178].

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