

## ON $(\lambda, \eta)(f)$ -STATISTICAL CONVERGENCE OF DOUBLE SEQUENCES IN 2-NORMED LINEAR SPACES

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*Abstract.* In this study, we utilize modulus functions under various conditions to define  $(\lambda, \eta)(f)$ -statistical convergence of double sequences in 2-normed linear spaces. Additionally, we explore the relationships between the sets of  $(\lambda, \eta)(f)$ -statistically convergent sequences and  $(\lambda, \eta)(f)$ -statistically bounded sequences in 2-normed linear spaces.

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