ON GENERALIZED β–ABSOLUTE CONVERGENCE OF SINGLE AND DOUBLE SERIES IN MULTIPLICATIVE SYSTEMS

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Abstract. In this paper, we obtain sufficient conditions for the generalized β-absolute convergence $(0 < \beta \leqslant 2)$ of single and double series in multiplicative systems of functions of generalized bounded fluctuation.

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