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ON UNIFORM CONVERGENCE OF TRIGONOMETRIC INTEGRAL–SERIES

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Abstract. In this paper, we give sufficient conditions for the uniform regular convergence of trigonometric integral-series, which are also necessary if the sequence of functions is non-negative. The new results also bring necessary and sufficient conditions for the uniform regular convergence of trigonometric integral-series in complex form.

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