

## LACUNARY STATISTICAL MEASURABLE CONVERGENCE WITH APPLICATION TO KOROVKIN-TYPE THEOREM

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*Abstract.* The purpose of the article is to investigate the concept of lacunary statistical mean convergence, lacunary statistical measurable convergence and lacunary statistical Lebesgue measurable convergence. We demonstrate an advanced perception to Korovkin-type theorem with the help of three algebraic test functions by means of lacunary statistical Lebesgue measurable convergence.

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