

## ON ABSOLUTE MATRIX SUMMABILITY METHODS

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*Abstract.* In this study, we have generalized Bor's theorems ([14]) for the absolute matrix summability method.

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