

APPLICATIONS OF AN IDENTITY OF BATIR

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Abstract. Based on an interesting identity of Batir we derive new identities for double sums involving famous number sequences. We also prove some double sum identities for binomial transform pairs.

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