

THE EQUIVALENCE BETWEEN MANN AND IMPLICIT MANN ITERATIONS

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Abstract. We shall prove the equivalence between the convergences of Mann and implicit Mann iterations dealing with various classes of non-Lipschitzian operators.

Mathematics subject classification (2000): 47H10.

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