

GENERALIZED WEIGHTED INEQUALITY WITH NEGATIVE POWERS

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Abstract. In this paper necessary and sufficient conditions for the validity of the generalized Hardy inequality for the case $-\infty < q \leq p < 0$ and $0 < p \leq q < 1$ are derived. Furthermore, some special cases are considered.

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