

## SOME MULTI-DIMENSIONAL HARDY TYPE INTEGRAL INEQUALITIES

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*Abstract.* In this paper we prove some new results concerning multi-dimensional Hardy type integral inequalities and also some corresponding limit Pólya–Knopp type inequalities.

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*Key words and phrases:* Integral inequalities, weights, multi-dimensional Hardy operator, multi-dimensional geometric mean operator.

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