

REVERSE WEIGHTED L_p -NORM INEQUALITIES AND THEIR APPLICATIONS

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Abstract. In this paper, we give the new type of reverse weighted L_p norm inequalities and their important applications to studying stability of some inverse problems. Especially, we will see their applications to inverse problems in non-homogeneous linear differential equations.

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