

SOME MORE INEQUALITIES FOR ARITHMETIC MEAN, HARMONIC MEAN AND VARIANCE

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Abstract. We derive bounds on the variance of a random variable in terms of its arithmetic and harmonic means. Both discrete and continuous cases are considered, and an operator version is obtained. Some refinements of the Kantorovich inequality are obtained. Bounds for the largest and smallest eigenvalues of a positive definite matrix are also obtained.

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