

AN EXTENSION OF THE HILBERT-TYPE INEQUALITY AND ITS REVERSE

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Abstract. By introducing some parameters and the weight coefficient, one proves a new extension of the Hilbert-type inequality with a best constant factor. The reverse, some equivalent forms and a number of new particular cases are considered.

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