

MULTIVARIATE MOMENT TYPE OPERATORS: APPROXIMATION PROPERTIES IN ORLICZ SPACES

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Abstract. In this paper modular convergence theorems in Orlicz spaces for multivariate extensions of the one-dimensional moment operator are given and the order of modular convergence in modular Lipschitz classes is studied.

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