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ON THE RASSIAS STABILITY OF A BI–JENSEN FUNCTIONAL EQUATION

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Abstract. In this paper, we investigate the stability of a bi-Jensen functional equation

$$4f\left(\frac{x+y}{2}, \frac{z+w}{2}\right) = f(x,z) + f(x,w) + f(y,z) + f(y,w)$$

in the sense of Th. M. Rassias. Also, we establish the superstability of a bi-Jensen functional equation.

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