

ON A QUADRATIC ESTIMATE OF SHAFER

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Abstract. In this note, a upper bound for $\arctan x$ is obtained. We would point out that the numbers $80/3$ and $256/\pi^2$ are the best constants in Shafer-type inequality.

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