

## AN INEQUALITY FOR POLYNOMIALS WITH POSITIVE COEFFICIENTS AND APPLICATIONS IN RATIONAL APPROXIMATION

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*Abstract.* We extend an inequality of Leviatan and Lubinsky ([3: Theorem 3.1]) to polynomials with positive coefficients. Two applications in approximation by rational functions with prescribed numerators are given.

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