

Q -NORM INEQUALITIES FOR SEQUENCES OF HILBERT SPACE OPERATORS

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Abstract. We give some inequalities related to a large class of operator norms, the so-called Q -norms, for a (not necessary commutative) family of bounded linear operators acting on a Hilbert space that are related to the classical Schwarz inequality. Applications for vector inequalities are also provided.

Mathematics subject classification (2000): 47A05, 47A12.

Keywords and phrases: Bounded linear operators, Hilbert spaces, Schwarz inequality, Commuting operators.

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