

## PARTIAL $\Delta$ -DIFFERENTIATION FOR MULTIVARIABLE FUNCTIONS ON $n$ -DIMENSIONAL TIME SCALES

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*Abstract.* The general idea of this paper is to study a differential calculus for multivariable functions on time scales. Such a calculus can be used to develop a theory of partial dynamic equations on time scales.

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