THE INTEGRAL VERSION OF POPOVICIU'S INEQUALITY

CONSTANTIN P. NICULESCU

Abstract. T. Popoviciu [7] has proved in 1965 an interesting characterization of the convex functions of one real variable, relating the arithmetic mean of its values and the values taken at the barycenters of certain subfamilies of the given family of points. The aim of our paper is to prove an integral analogue.

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