

BOOTSTRAPPING WEIGHTED FOURIER INEQUALITIES

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Abstract. The theory of positive integral operators is applied to convolution operators, giving a method of producing new weighted Fourier inequalities from known ones. The new inequalities produced depend on six parameters; two real indices, two complex-valued measures, and two positive functions. The method may be iterated using the last inequality generated as input to the next stage.

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