CHARACTERIZATION OF THE NORM TRIANGLE EQUALITY
IN PRE–HILBERT C^*–MODULES AND APPLICATIONS

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Abstract. The characterization of the norm triangle equality in pre-Hilbert C^*-modules is given. The result is applied for describing the case of equality in some generalizations of the Dunkl-Williams inequality.

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