INEQUALITIES INVOLVING THE
KHATRI–RAO PRODUCT OF MATRICES

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Abstract. We shall show several complementary inequalities to Jensen's type inequality involving the Khatri-Rao product of maps on positive definite matrices. They are applied to extend some known inequalities involving powers of the Khatri-Rao product. Finally, we have generalized some known results for the Hadamard product of operators.

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