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INEQUALITIES OF THE DUNKL–WILLIAMS TYPE FOR ABSOLUTE VALUE OPERATORS

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Abstract. In this paper we give operator-valued versions of some Dunkl-Williams related inequalities for Hilbert space operators. The case of equality is also studied.

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