

EXTENDED CESÁRO OPERATORS ON BMOA SPACES IN THE UNIT BALL

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Abstract. Let g be a holomorphic map of B , where B is the unit ball of C^n . This paper gives necessary and sufficient conditions for the extended Cesáro operators induced by g to be bounded or compact on BMOA.

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