

SOME SUBCLASSES OF MULTIVALENT FUNCTIONS INVOLVING THE EXTENDED FRACTIONAL DIFFERINTEGRAL OPERATOR

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Abstract. The object of the present paper, is to investigate various properties of several subclasses of multivalent analytic functions which are defined here by using the extended fractional differintegral operator

$$\Omega_z^{(\lambda, p)} \quad (-\infty < \lambda < p + 1; p \in \mathbb{N}).$$

Mathematics subject classification (2010): 30C45.

Keywords and phrases: Analytic functions, p -valent functions, differintegral operator.

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