

BOUNDEDNESS FOR MULTILINEAR OPERATORS OF PSEUDO-DIFFERENTIAL OPERATORS FOR THE EXTREME CASES

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Abstract. We prove the boundedness of the multilinear operators associated to the pseudo-differential operator for the extreme cases.

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