

## NONLINEAR PARABOLIC INEQUALITIES ON A GENERAL CONVEX DOMAIN

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*Abstract.* The paper deals with the existence and uniqueness of solutions of some non linear parabolic inequalities in the Orlicz-Sobolev spaces framework.

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