

BOUNDS IMPROVEMENT FOR ALTERNATING MATHIEU TYPE SERIES

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Abstract. The aim of this research paper is to establish some precise, new bounding inequalities for the generalized alternating Mathieu series using their integral representations and the classical CBS inequality. The obtained inequalities improve certain bounds derived recently by Tomovski and Hilfer in [17].

Mathematics subject classification (2010): Primary 26D15, 33C60; Secondary 33E20, 44A20.

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