

SOME BETTER BOUNDS ON THE VARIANCE WITH APPLICATIONS

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Abstract. We derive bounds on the variance of a finite universe. Some related inequalities for the roots of the polynomial equations and bounds for the largest and smallest eigenvalues of a square matrix with real spectrum are obtained.

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