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A GOOD λ ESTIMATE FOR MULTILINEAR COMMUTATOR OF FRACTIONAL INTEGRAL ON SPACES OF HOMOGENEOUS TYPE

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Abstract. In this paper, a good λ estimate for the multilinear commutator associated to the fractional integral operator on the spaces of homogeneous type is obtained. Under this result, we get the $(L^p(X), L^q(X))$-boundedness of the multilinear commutator.

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