

ON BERGSTROM INEQUALITY FOR COMMUTING GRAMIAN NORMAL OPERATORS

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Abstract. We hereby present a variant of Bergstrom inequality for gramian normal operators on Loynes spaces and Hilbert spaces, as well as several consequences.

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