

ITERATIVE APPROXIMATIONS FOR A FAMILY OF MULTIVALUED MAPPINGS IN BANACH SPACES

ZHANFEI ZUO

Abstract. In this paper we consider the convergence of iterative processes for a family of multivalued nonexpansive mappings. Under somewhat different conditions the sequences of Noor, Mann and Ishikawa iterates converge to the common fixed point of the family of multivalued nonexpansive mappings.

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