

A COROLLARY OF ALEXANDER'S INEQUALITY

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Abstract. A simple corollary of Alexander's inequality is shown for a uniform algebra. As a result, we give an inequality between the L^∞ -type norm of a given analytic function and the L^1 -type norm of the derivative.

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