

ON SOME INEQUALITIES FOR DERIVATIVES OF POLYNOMIALS AND RATIONAL FUNCTIONS

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Abstract. Using methods of geometric function theory, we get new inequalities for derivatives of polynomials and rational functions. These theorems refine and supplement some known results.

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