

EXPONENTIAL CONVEXITY AND JENSEN'S INEQUALITY FOR DIVIDED DIFFERENCES

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Abstract. In this paper we obtain means which involve divided differences for n -convex functions. We examine their monotonicity property using exponentially convex functions.

Mathematics subject classification (2010): 26D15, 26D20, 26D99.

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