

ALTERNATIVE REVERSE INEQUALITIES FOR YOUNG'S INEQUALITY

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Abstract. Two reverse inequalities for Young's inequality were shown by M. Tominaga, using Specht ratio. In this short paper, we show alternative reverse inequalities for Young's inequality without using Specht ratio.

Mathematics subject classification (2010): 15A39, 15A45.

Keywords and phrases: Operator inequality, Young's inequality, reverse inequality and positive operator.

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