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HARDY INEQUALITIES FOR SOME NON–CONVEX DOMAINS

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Abstract. Considering two different geometrical conditions, we obtain some new Hardy-type inequalities for non-convex domains in $\mathbb{R}^n$. In order to do so, we study the three-dimensional case and then generalise the approach to the n-dimensional case.

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