

GENERALIZED HILBERT OPERATORS ON WEIGHTED MORREY–HERZ SPACES

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Abstract. This paper give some necessary and sufficient conditions for the generalized Hilbert operators to be bounded on the weighted Morrey–Herz spaces. The corresponding new operator norm inequalities are obtained.

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