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A REMARK ON EXTENSION OF ORDER PRESERVING OPERATOR INEQUALITY

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Abstract. We will give an extension of order preserving operator inequality of Furuta type.

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