

## AN INEQUALITY FOR THE GAMMA FUNCTION CONJECTURED BY D. KERSHAW

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*Abstract.* We prove the inequality  $\Gamma(x) + \Gamma(1/x) \leq \Gamma(1+x+1/x)$ .

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