INTEGRABILITY THEOREMS FOR FOURIER–JACOBI TRANSFORMS

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Abstract. In this paper, we prove the Hardy-Littlewood-Paley inequality for the generalized Fourier transform on Chébli-Trimèche hypergroups and we study in the particular case of the Jacobi hypergroup the integrability of this transform on Besov-type spaces.

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