

THE JENSEN INEQUALITY IN AN EXTERNAL FORMULA

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Abstract. The classical Jensen inequality is expressed by internally dividing points and so is non-commutative Jensen inequalities. In this paper, considering that it is expressed by externally dividing points, we shall discuss two non-commutative Jensen inequalities and their reverse, that is, one is a vector state version and the other is a Davis-Cho-Jensen type version.

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