MIXED SYMMETRIC MEANS RELATED TO
THE CLASSICAL JENSEN'S INEQUALITY

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Abstract. In this paper, we define some new mixed symmetric means corresponding to various refinements of classical Jensen's inequality. A new refinement of classical Jensen's inequality is given. We also prove the n-exponential convexity for the functionals constructed from the refinement results. In the end some applications are discussed.

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