

OPERATOR MONOTONE FUNCTIONS, $A > B > 0$ AND $\log A > \log B$

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Abstract. Let $f(t)$ be any non-constant operator monotone function on $[0, \infty)$ and also let A and B be strictly positive operators on a Hilbert space H .

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