

A MULTIPLE OPIAL TYPE INEQUALITY FOR THE RIEMANN–LIOUVILLE FRACTIONAL DERIVATIVES

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Abstract. The aim of this paper is to prove a multiple Opial type inequality for RL fractional derivatives which is proved for two factors and ordinary derivatives by Fink in [6]. Two methods are applied and a comparison of the obtained estimations is also given.

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